

## Massive Open Online Course Resilience, Sustainability & Digitalisation in Critical Infrastructure

### Lecture 3 Resilience assessment

#### Lecture Notes

This project has received funding from the Horizon Europe Programme under the Marie Skłodowska-Curie Staff Exchanges Action (GA no. 101086413).

Co-funded by the UK Research & Innovation, and the Swiss State Secretariat for Education, Research & Innovation.



## Introduction

A Massive Open Online Course (MOOC) is a free, open, online course designed to offer a taste of higher education to learners from across the world. The University of Birmingham is delivering new MOOCs in partnership with FutureLearn. Delivered by world-class academics from the University of Birmingham and other partners of the HORIZON Recharged project (GA no. 101086413), the course enable learners worldwide to sample high-quality academic content via an interactive web-based platform from leading global universities, increasing access to higher education for a whole new cohort of learners.

The course is developed by senior academic staff and their content is reviewed regularly, taking into account student feedback.

This MOOC brings together world experts, including general audiences, aiming to provide training with life-long updates and professional development opportunities for general and specialised audiences. The MOOC contains all the necessary components of a university taught module, e.g. prerequisites, content and aims, learning outcomes, attributes for sustainable professional development (cognitive, analytical, transferable skills, professional and practical skills), expected hours of study, assessment patterns, units of assessment and reading list, warm-up sessions, with relevant podcasts and videos, lecture notes and recorded lectures, some of which will be tailored for general audiences. This open course will be available on [futurelearn.com](https://futurelearn.com) and on the [project website](#).

These lecture notes are accompanying the seven lectures of the MOOC. Following is the MOOC description, which contains the outcomes, the aims per week and the learning activities. The latter include a combination of material acquisitions and discussions, investigations and production, practical examples and analysis of case studies, and a set of collaboration and discussion forum.

## Outcomes

### Lecture 3-Week 3

The aim of this week is to introduce the concept and properties of resilience for critical infrastructure, including quantification of resilience based on metrics for decision making. This week also includes definition of restoration and reinstatement models considering available resources, level of damage and type of infrastructure assets. The concepts of proactive (ex-ante / by design) and reactive (ex-post/ by intervention) resilience will be presented based on case studies for critical assets. Resilience by assessment will be discussed as a capability in case of inaccessible assets.

- Define resilience and its properties, restoration and reinstatement models, considering temporal and spatial variabilities.
- Define proactive and reactive restoration at asset and system level.
- Define resilience metrics for decision-making.

Present case studies on quantification of resilience for critical infrastructure exposed to different hazard scenarios.

## Lecture 3. Resilience assessment

Lecture 3  
Massive Open Online Course  
Resilience, Sustainability & Digitalisation in Critical Infrastructure

### Resilience assessment

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#### Lecture 3 Outcomes

- Define resilience and its properties, restoration and reinstatement models, considering temporal and spatial variabilities.
- Define proactive and reactive restoration at asset and system level.
- Define resilience metrics for decision-making.
- Present case studies on quantification of resilience for critical infrastructure exposed to different hazard scenarios.



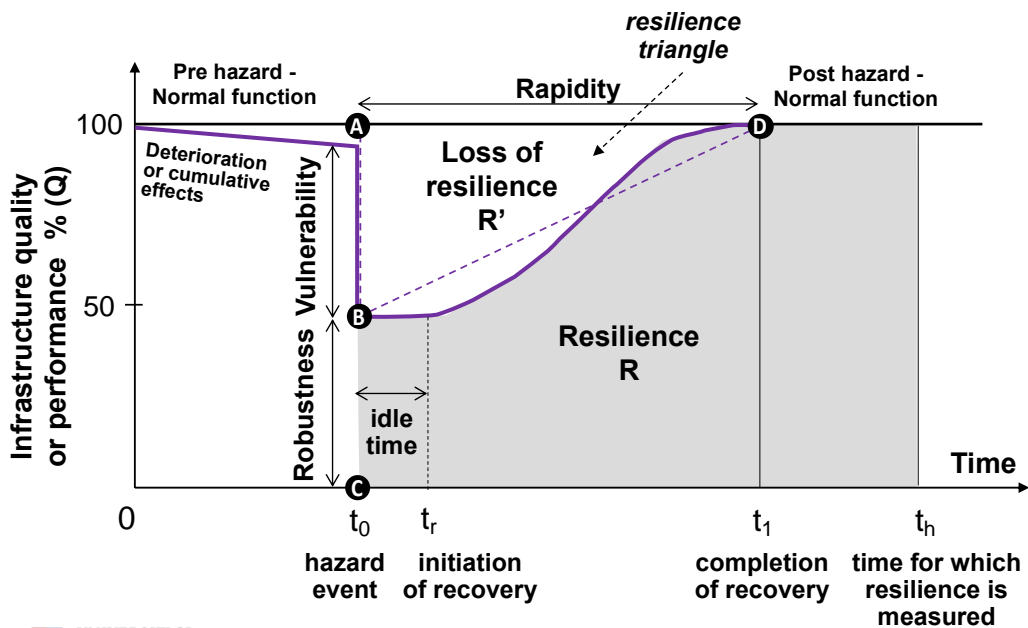
## Activity 1. Restoration and reinstatement models

### ACTIVITY 1: Restoration and reinstatement models

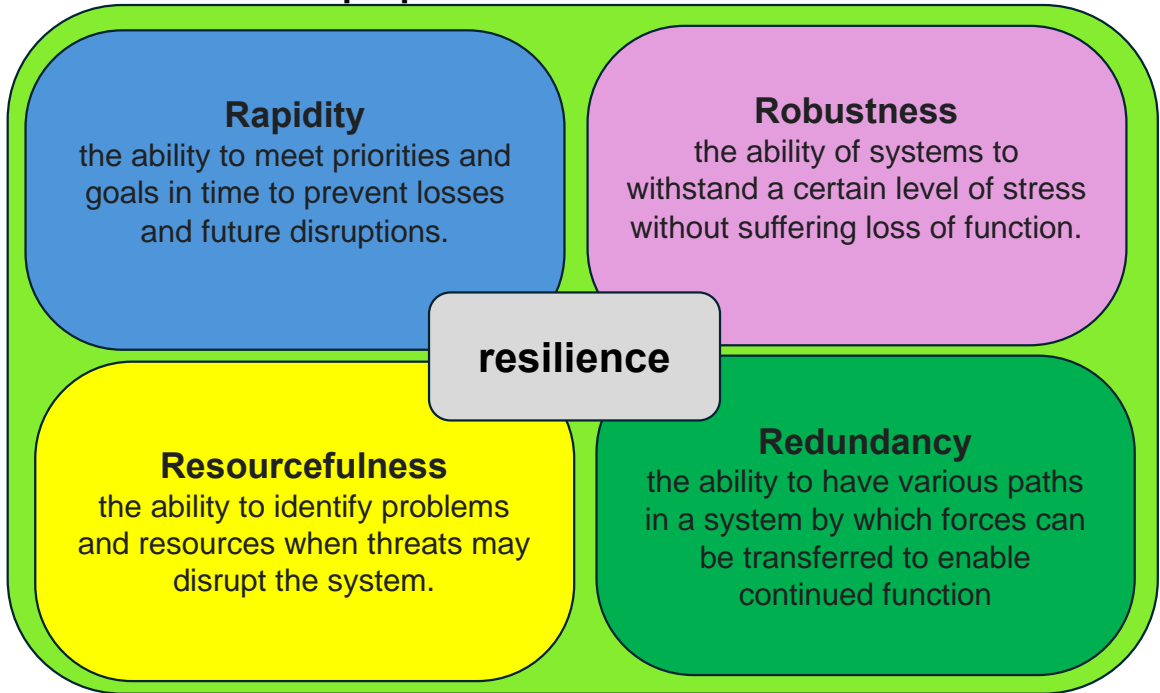
- Define resilience and its properties
- Restoration and reinstatement models
- Restoration vs reinstatement
- Temporal and spatial variabilities and other uncertainties



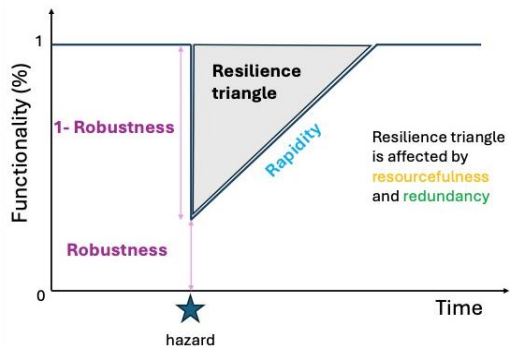
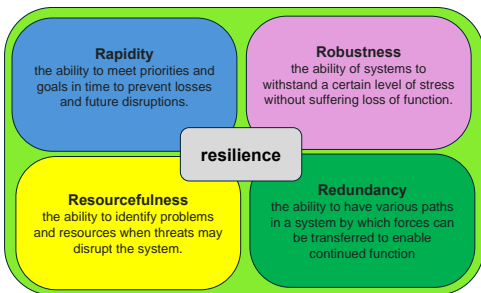
### Resilience assessment



### Define resilience and its properties



### The attributed of resilience - the 4Rs (Bruneau et al. 2003)



**Different scales:** from micro-to macro scale

**Bottom-up approach:**

component → asset → network → system → system of systems → regional → national → international

**Top-down approach:**

international → national → regional → system of systems → system → network → asset → component



## Restoration and reinstatement models

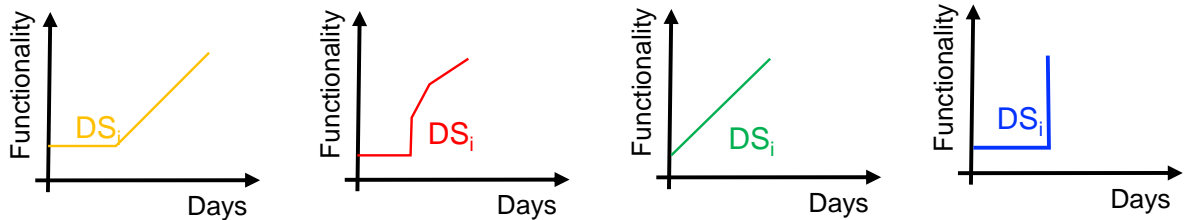
### Quantification of resilience

**robustness of structure, rapidity of restoration, resilience indices, examples**

**Resilience:** the capacity to recover quickly from catastrophic events.

Usually **recovery functions** are defined for different hazards and damage states, and thus combined to derive the **resilience curve** of a structural system.

Different **functional forms** can be adopted to characterise recovery functions.

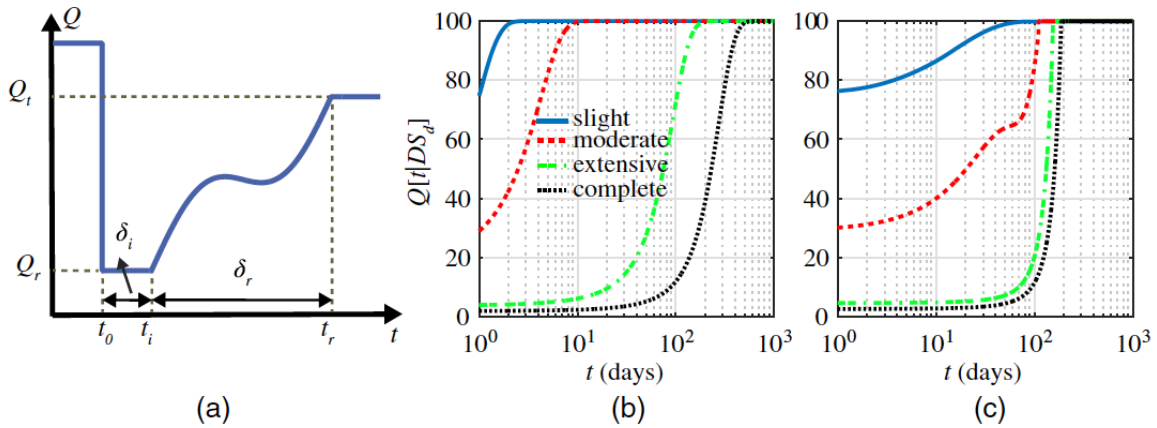


... or continuous functional forms usually representative of cumulative probability density function. This is convenient since it allows characterising recovery only defining few parameters.



## Restoration and reinstatement models

### Restoration curves



- (a) illustration of functionality recovery process
- (b) Hazus (2011)
- (c) Multi-parameter sinusoidal model (Bocchini et al.)

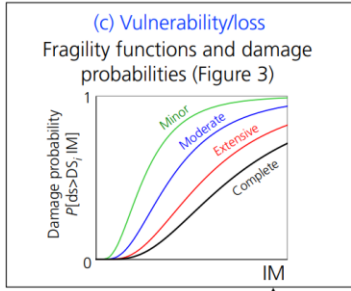


**4R** : Robustness, Redundancy, Resourcefulness, Rapidity

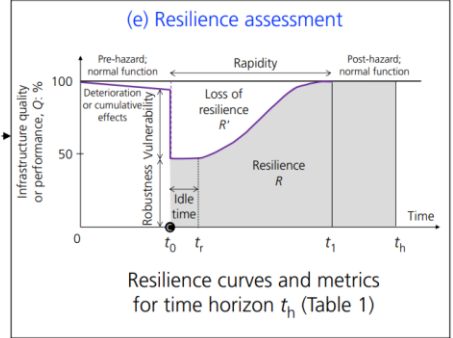
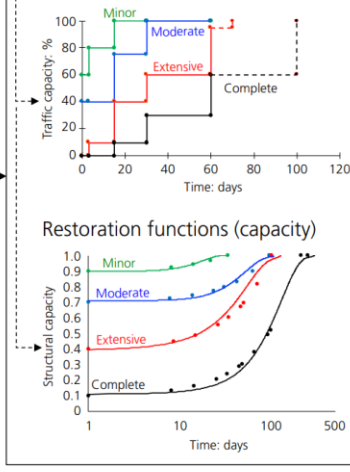
### Restoration and reinstatement models

(a) **Typology**  
Asset characteristics (e.g. material, type of piers/abutments/deck/foundations, design specifications)

(b) **Hazard**  
Hazard maps, intensity measures (IM) (e.g. PGA, scour depth, flow depth, water velocity)



(d) **Asset/network recovery**  
Measure of performance reinstatement functions (functionality) (Figure 4)



Argyroudis, 2021



### Restoration vs reinstatement

#### Survey for bridge restoration after flood

| damage level (DL)<br>(see Table 1 for description) | idle time in days<br>(before any restoration works) |     | reinstatement time in days (after the initiation of the restoration works) |    |     |   |    |     |   |    |     |   |    |     |   |    |     | restoration tasks & prioritisation<br>(see Table 3) | cost ratio (% of replacement cost of the bridge) |     |   |    |     |                                    |    |  |  |  |  |
|--|---|-----|--|----|-----|---|----|-----|---|----|-----|---|----|-----|---|----|-----|---|--|-----|---|----|-----|------------------------------------|----|--|--|--|--|
|  | min   | max | 0  |    |     |   |    | 3   |   |    |     |   | 15 |     |   |    |     |   |  | 30  |   |    |     |                                    | 60 |  |  |  |  |
|  |   |     | % traffic capacity of the bridge after damage                              |    |     |   |    |     |   |    |     |   |    |     |   |    |     |   |  |     |   |    |     |                                    |    |  |  |  |  |
| (1)  | (2)   | (3) | (4) (check mark "X")   |    |     |   |    |     |   |    |     |   |    |     |   |    |     | (5)   | (6)  |     |   |    |     |                                    |    |  |  |  |  |
|  |   |     | 0  | 50 | 100 | 0 | 50 | 100 | 0 | 50 | 100 | 0 | 50 | 100 | 0 | 50 | 100 | 0   | 50   | 100 | 0 | 50 | 100 |                                    |    |  |  |  |  |
| minor  | 4   | 14  |  | X  |     |   |    | X   |   |    | X   |   |    | X   |   |    | X   |   |  | X   |   |    | X   | R12, R5                            | 5  |  |  |  |  |
| moderate   | 10  | 30  | X  |    |     | X |    |     | X |    |     | X |    |     | X |    |     | X   |  |     | X |    |     | R1, R12, R5                        | 8  |  |  |  |  |
| extensive  | 25  | 45  | X  |    |     | X |    |     | X |    |     | X |    |     | X |    |     | X   |  |     | X |    |     | R1, R6, R12, R14, R2, R16, R5      | 15 |  |  |  |  |
| severe   | 30  | 70  | X  |    |     | X |    |     | X |    |     | X |    |     | X |    |     | X   |  |     | X |    |     | R1, R6, R12, R14, R2, R16, R15, R5 | 30 |  |  |  |  |

comments:

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## Restoration vs reinstatement

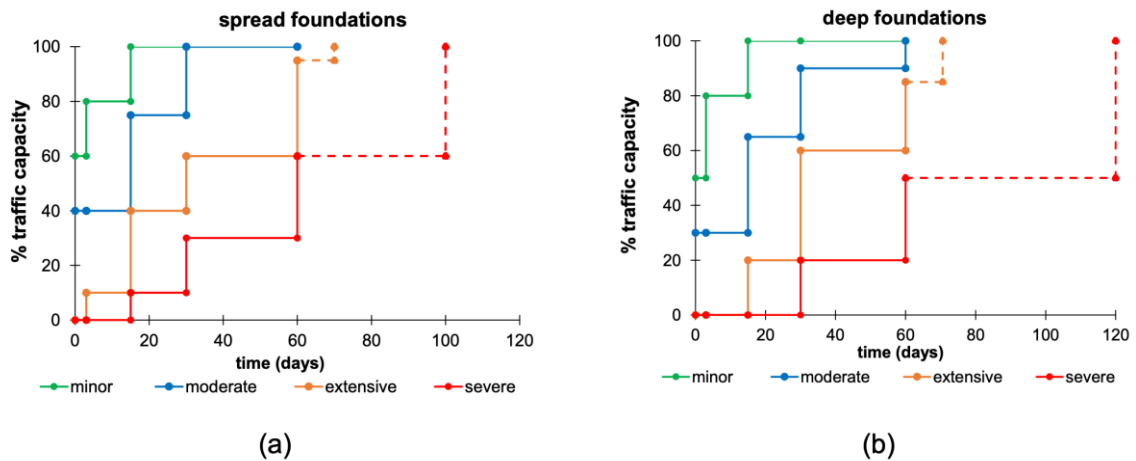
### Survey results and processing

| code<br>(1) | restoration task<br>(2)   | duration (days) |                |             |                | weighting factors |                 |                  |                |
|-------------|---|-----------------|----------------|-------------|----------------|-------------------|-----------------|------------------|----------------|
|             |   | minimum<br>(3)  | maximum<br>(4) | mean<br>(5) | std dev<br>(6) | minor<br>(7)      | moderate<br>(8) | extensive<br>(9) | severe<br>(10) |
| R0          | no action is required   | na              | na             | na          | na             | na                | na              | na               | na             |
| R1          | armouring countermeasures and flow-altering/cofferdam             | 5.6             | 24.8           | 15.2        | 13.4           | 0.7               | 0.8             | 0.9              | 1.0            |
| R2          | temporary support per pier  | 3.2             | 9.2            | 6.2         | 4.2            | 0.7               | 0.8             | 0.9              | 1.0            |
| R3          | temporary support of one abutment                                 | 3.0             | 10.0           | 6.5         | 4.6            | 0.7               | 0.8             | 0.9              | 1.0            |
| R4          | temporary support of one deck span /segment (midspan or support)  | 3.6             | 10.8           | 7.2         | 3.9            | 0.7               | 0.8             | 0.9              | 1.0            |
| R5          | repair cracks and spalling with epoxy and/or concrete             | 3.4             | 19.0           | 11.2        | 13.0           | 0.5               | 0.7             | 0.85             | 1.0            |
| R6          | re-alignment and/or leveling of pier                              | 12.0            | 29.8           | 20.9        | 23.6           | 0.5               | 0.7             | 0.85             | 1.0            |
| R7          | re-alignment of bearings  | 2.8             | 10.0           | 6.4         | 6.8            | 1.0               | 1.0             | 1.0              | 1.0            |
| R8          | jacketing or local strengthening (pier or abutment or foundation) | 11.4            | 35.0           | 23.2        | 30.0           | 0.0               | 0.4             | 0.7              | 1.0            |
| R9          | jacketing or local strengthening (deck)                           | 13.8            | 32.8           | 23.3        | 23.3           | 0.0               | 0.4             | 0.7              | 1.0            |
| R10         | re-alignment of deck segment                                      | 8.2             | 18.2           | 13.2        | 17.9           | 0.5               | 0.7             | 0.85             | 1.0            |
| R11         | erosion protection measures rip-rap and/or gabions for            | 6.8             | 16.3           | 11.5        | 6.4            | 0.7               | 0.8             | 0.9              | 1.0            |
| R12         | filling of scour hole and scour protection                        | 6.0             | 23.4           | 14.7        | 13.5           | 0.7               | 0.8             | 0.9              | 1.0            |
| R13         | removal of debris   | 2.9             | 7.4            | 5.2         | 4.7            | 0.7               | 0.8             | 0.9              | 1.0            |
| R14         | ground improvement per foundation                                 | 11.2            | 32.0           | 21.6        | 21.8           | 0.7               | 0.8             | 0.9              | 1.0            |
| R15         | installation or retrofitting of deep foundation system            | 33.8            | 66.0           | 49.9        | 49.3           | 1.0               | 1.0             | 1.0              | 1.0            |
| R16         | extension of foundation footing                                   | 20.8            | 46.0           | 33.4        | 32.1           | 1.0               | 1.0             | 1.0              | 1.0            |
| R17         | reconstruction/replacement of the abutment and wingwalls          | 31.0            | 72.0           | 51.5        | 41.1           | 1.0               | 1.0             | 1.0              | 1.0            |
| R18         | reconstruction/replacement of the pier                            | 42.0            | 78.0           | 60.0        | 44.3           | 1.0               | 1.0             | 1.0              | 1.0            |
| R19         | temporary support and replacement of the bearings                 | 3.8             | 9.4            | 6.6         | 3.8            | 1.0               | 1.0             | 1.0              | 1.0            |
| R20         | replacement of the backfill and approach slab and mudjacking      | 12.0            | 32.0           | 22.0        | 11.5           | 1.0               | 1.0             | 1.0              | 1.0            |
| R21         | replacement of expansion joint                                    | 2.0             | 7.2            | 4.6         | 3.1            | 0.5               | 0.7             | 0.85             | 1.0            |
| R22         | demolish/replacement of a deck span/segment                       | 22.2            | 51.0           | 36.6        | 23.2           | 1.0               | 1.0             | 1.0              | 1.0            |
| R23         | demolish/replacement (part) of the bridge                         | 88.8            | 334.0          | 211.4       | 133.8          | 1.0               | 1.0             | 1.0              | 1.0            |
| R24         | please add customised task  | -               | -              | -           | -              | -                 | -               | -                | -              |



## Restoration vs reinstatement

### Survey results: reinstatement models



**Figure 3.** Reinstatement models illustrating the post-flood gain of the traffic capacity (%) of the bridge for spread (a) and deep (b) foundation (dashed lines is a projection based on judgment).

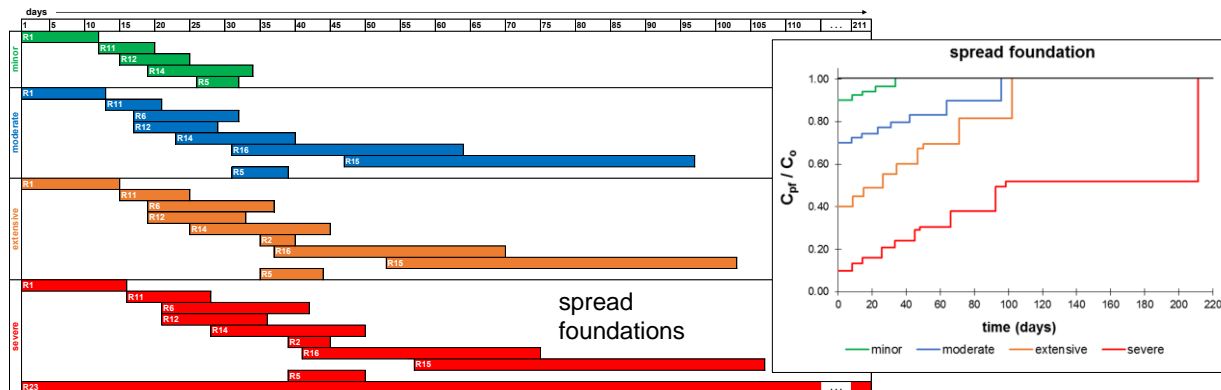
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## Restoration vs reinstatement

### Restoration task prioritisation, dependencies, durations & models

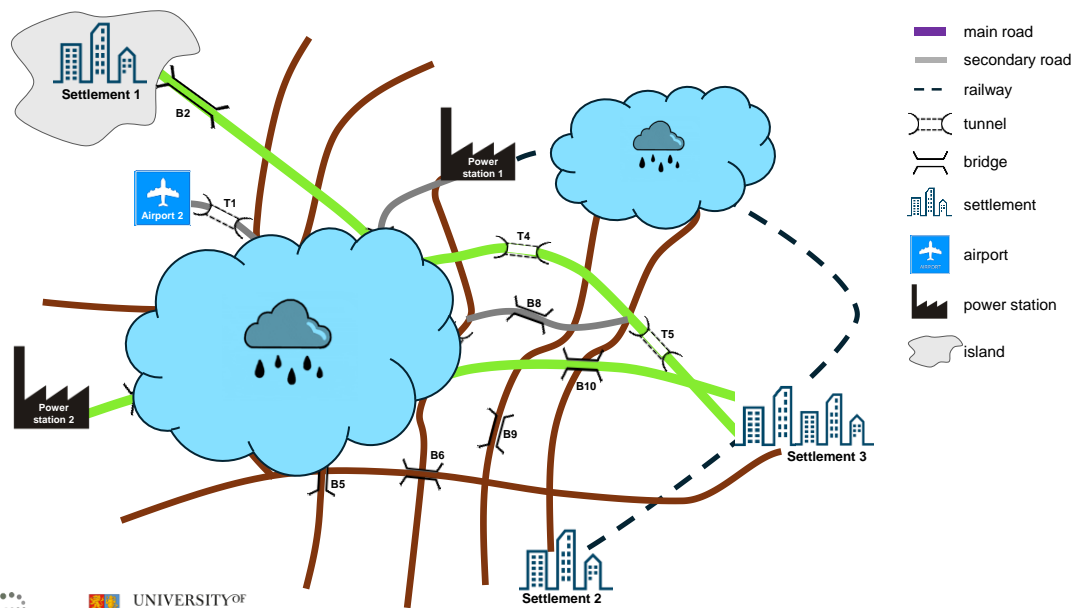


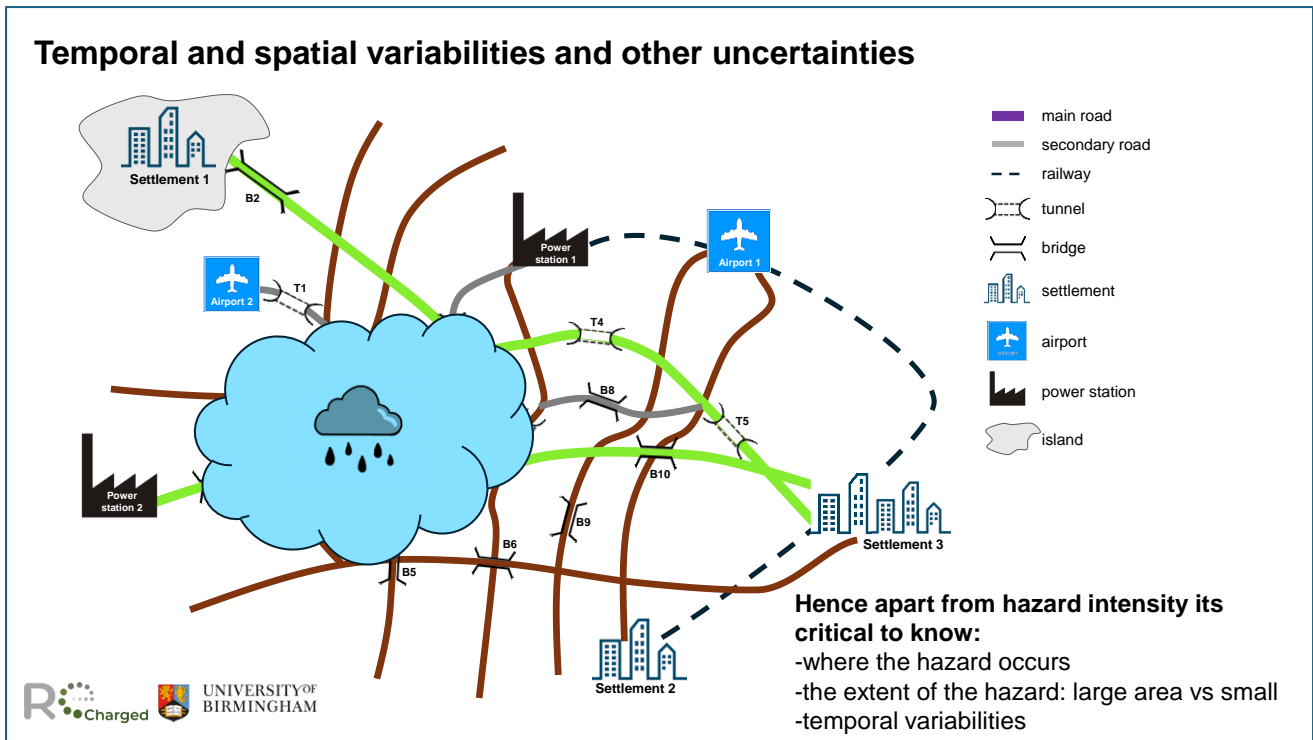
Stepwise restoration models illustrating the ratio of the post-flood bridge capacity ( $C_{pt}$ ) over the original capacity ( $C_o$ )

Mitoulis et al. 2021



## Temporal and spatial variabilities and other uncertainties





The two slides above illustrate conceptual maps highlighting the importance of understanding temporal and spatial variabilities and other uncertainties related to hazards for our resilience assessments.

### Components of the Map:

#### 1. Routes and Infrastructure:

- **Main Roads:** Indicated by thick purple lines.
- **Secondary Roads:** Represented by thinner gray lines.
- **Railways:** Depicted by dashed lines.
- **Tunnels:** Shown as connected double lines (T1, T4, T5).
- **Bridges:** Represented by parallel lines with a gap (B2, B5, B6, B8, B9, B10).

#### 2. Key Locations:

- **Settlements:** Illustrated with building icons and labelled as Settlement 1, Settlement 2, and Settlement 3.
- **Airports:** Depicted with airplane icons and labelled as Airport 1 and Airport 2.
- **Power Stations:** Represented with factory icons and labelled as Power station 1 and Power station 2.
- **Island:** Shown as a landmass shape.

#### 3. Hazard Representation:

- Cloud with raindrops symbolizing a hazard event affecting the area, placed centrally on the map.

### Points of Interest:

- The green lines appear to denote critical routes or pathways impacted by the hazard.
- The connections between different infrastructures (e.g., roads, railways, bridges, tunnels) suggest a complex network affected by the hazard.

- The description emphasizes the importance of knowing:
  - **Where the hazard occurs**
  - **The extent of the hazard (large area vs. small area)**
  - **Temporal variabilities (time-related changes)**

This map serves to emphasize the necessity of understanding the spatial distribution and temporal aspects of hazards, focusing on how they impact various infrastructural elements and settlements. It highlights the interconnected nature of these elements and the critical information required to manage and mitigate hazards effectively.

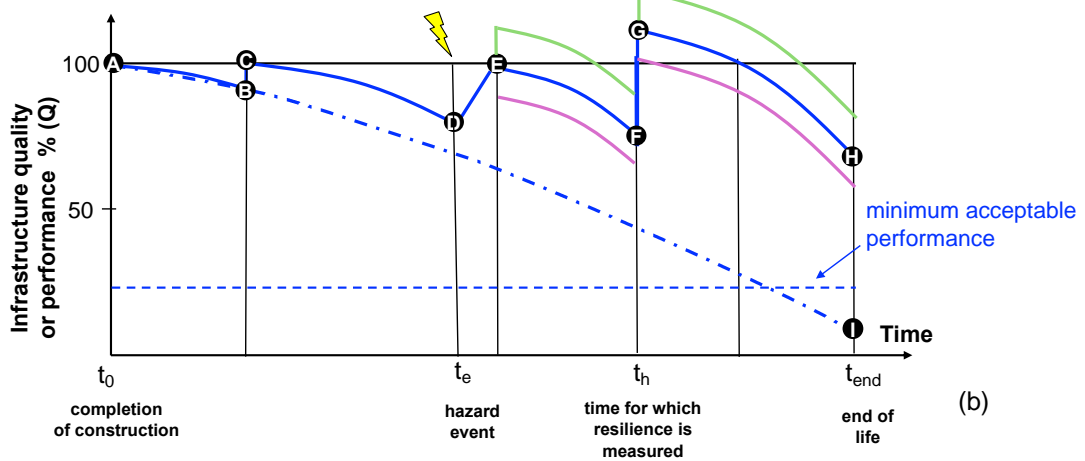
## Activity 2. Proactive and reactive restoration

### ACTIVITY 2: Proactive and reactive restoration

- Proactive (ex-ante) vs. reactive (ex-post) and comparisons strategies
- Adaptation strategies



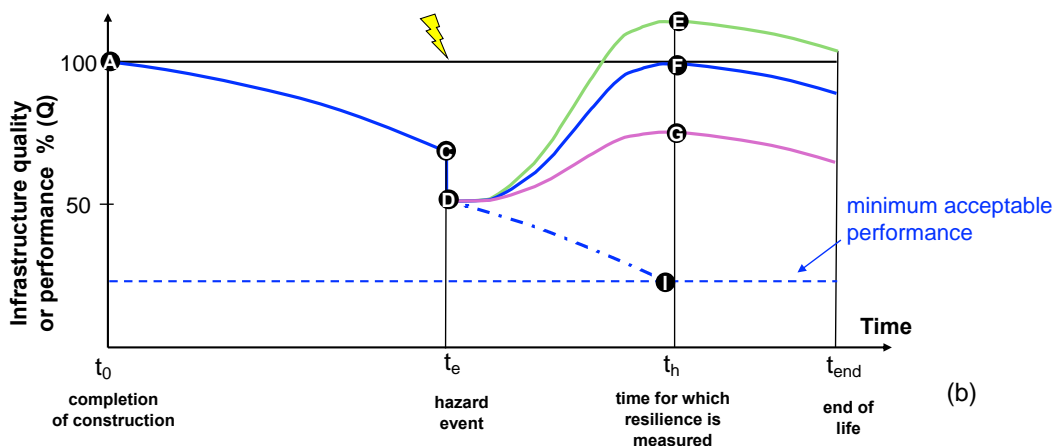
### Proactive (ex-ante) vs. reactive (ex-post) and comparisons strategies Proactive / preventive maintenance / adaptation before the threat



- AI:** deterioration of infrastructure quality throughout its life
- BC:** proactive adaptation measures and/or maintenance
- CD:** deterioration of infrastructure
- DE:** restoration after a climate hazard occurrence (see Fig. 1, C to F)
- FG:** enhancement of infrastructure performance with adaptation measures
- GH:** operation until the end of life



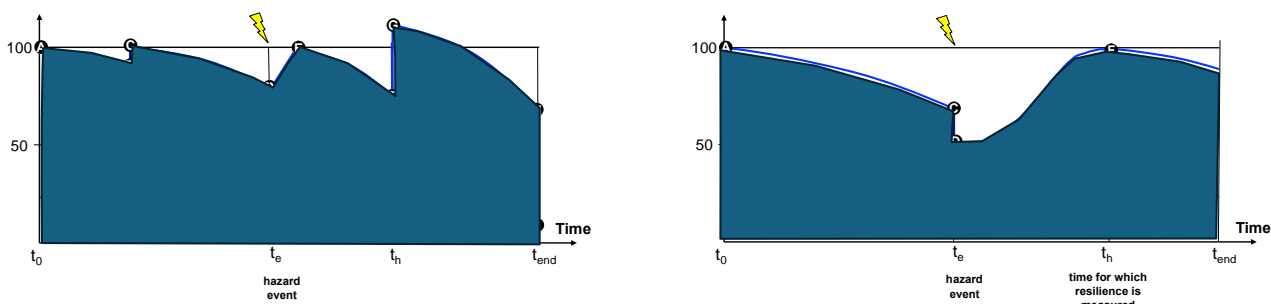
### Proactive (ex-ante) vs. reactive (ex-post) and comparisons strategies Reactive / corrective maintenance/adaptation before the threat



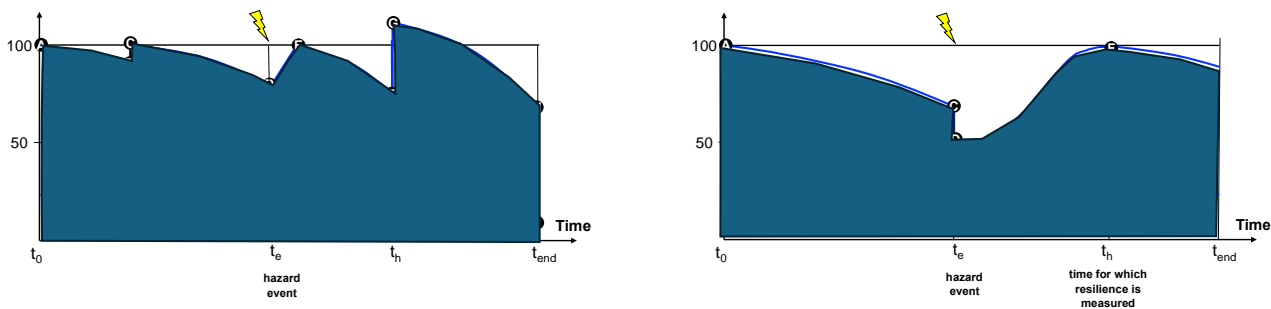
- AI: deterioration of infrastructure quality throughout its life
- CD: loss of performance due to hazard occurrence
- DG: reactive measures, partially restored
- DF: reactive measures, fully restored
- DE: reactive and adaptation measures beyond the original capacity



### Proactive (ex-ante) vs. reactive (ex-post) and comparisons strategies



### Proactive (ex-ante) vs. reactive (ex-post) and comparisons strategies



### Adaptation strategies

#### EU Strategy on Adaptation to Climate Change - Policy context

- The 2030 Agenda for Sustainable Development
- The Paris Agreement
- The European Green Deal:

- European Climate Law,                      • 2030 Climate Target Plan
- European Climate Pact                      • EU Biodiversity strategy
- Farm to fork strategy                      • Forest strategy
- Renewed sustainable finance strategy
- ... and more!



## Adaptation strategies

### EU Strategy on Adaptation to Climate Change - Vision & Objectives

- Vision: by 2050 the EU will be a climate-resilient society, fully adapted to the unavoidable impacts of climate change
- Objectives:
  - **Smarter adaptation** – improving knowledge and managing uncertainty
  - **More systemic adaptation** – support policy development at all levels and sectors
  - **Faster adaptation** – speeding up adaptation across the board
  - **Stepping up international action** for climate resilience



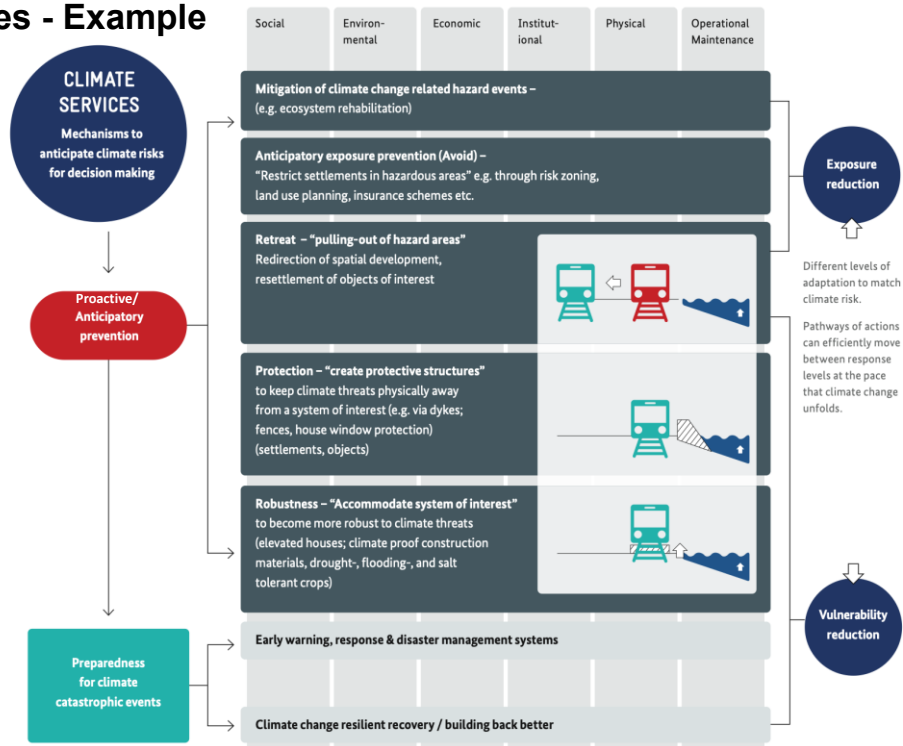
© picture: Peter Löffler



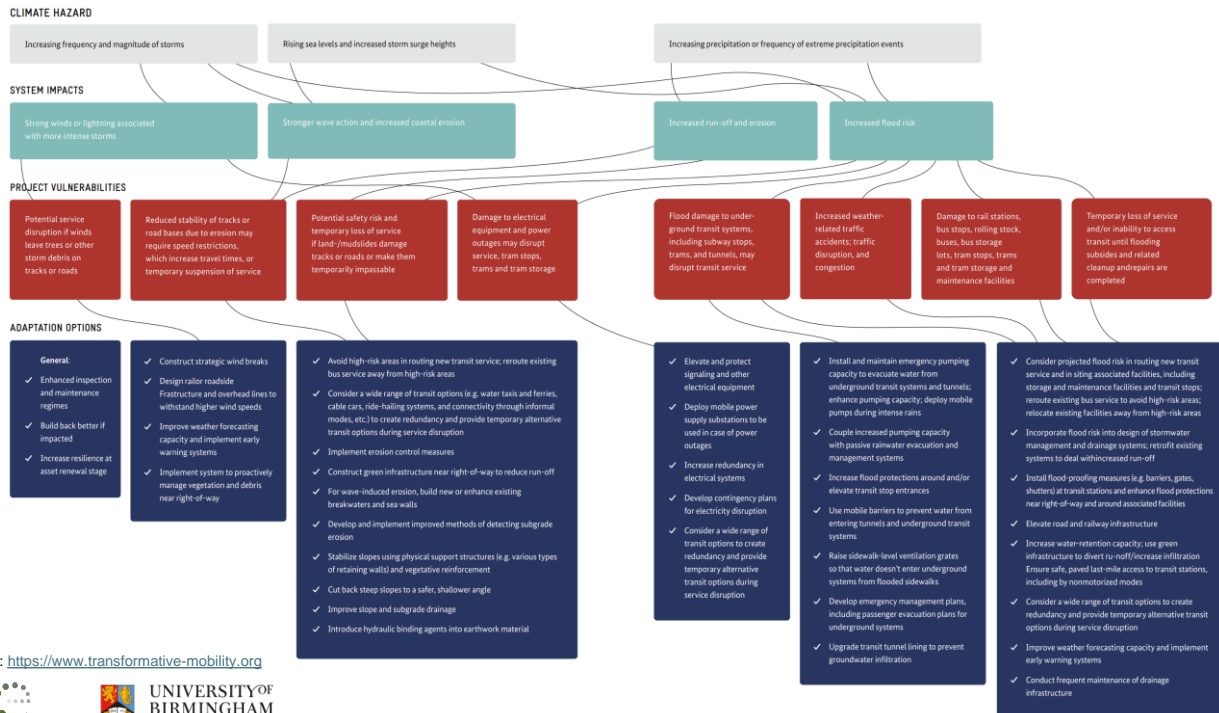
## Adaptation strategies - Example

### Climate risk management approaches at different levels of climate change

source: <https://www.transformative-mobility.org>



## Adaptation strategies - Decision tree for urban mass transit projects



## Comparisons of ex-ante and ex-post strategies

### Discussion:

- Can you think of qualitative examples where proactive strategies would be more efficient and cost effective to reactive strategies?



## Activity 3. Resilience metrics

### ACTIVITY 3: Resilience metrics

- Resilience metrics
- Resilience-based decision making
- Case studies



### Resilience metrics

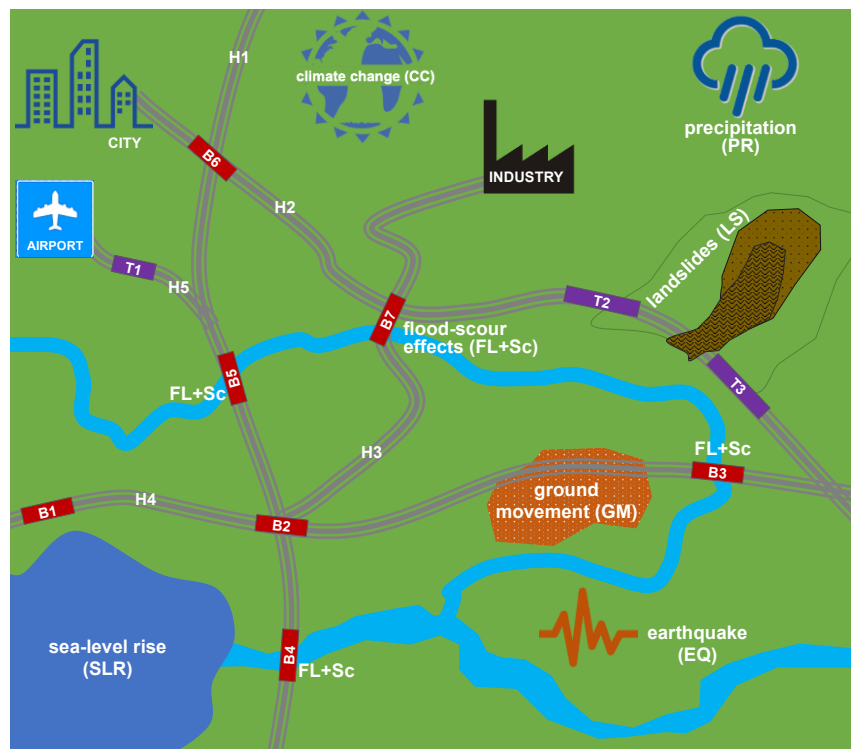
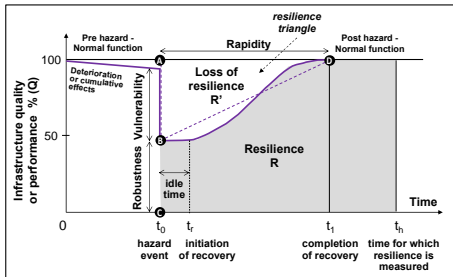


Figure 1: Resilience model



## Resilience metrics



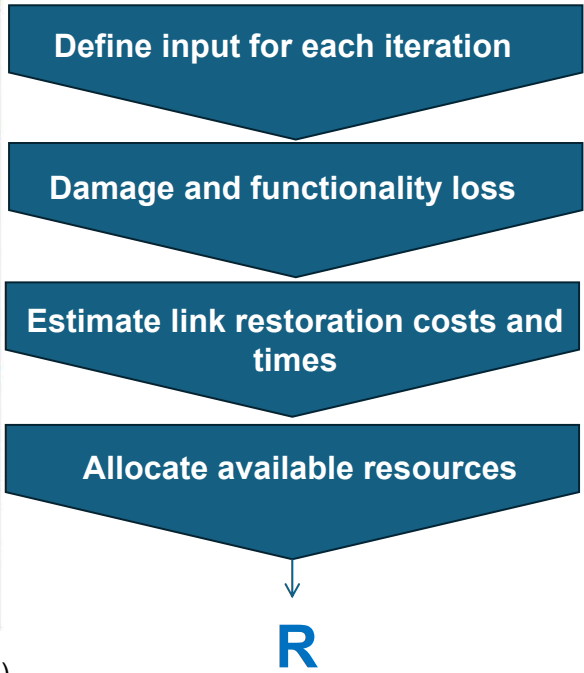
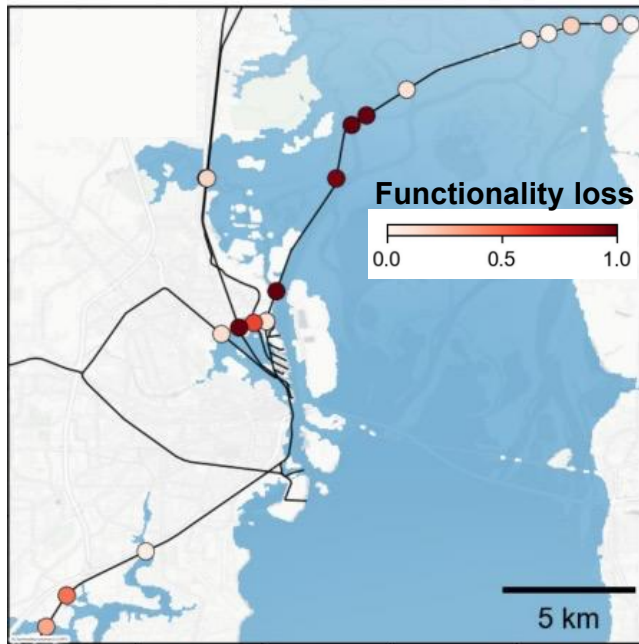
| reference                   | mathematical formulation                                      | parameters of the resilience metric   | comments and/or advantages & disadvantages  |
|-----------------------------|---|---|---|
| Ayyub (2014)                | Robustness = B - C<br>Rapidly = $\frac{A-B}{t_1-t_0}$         | See Figure 1  | Robustness units: percentage<br>Rapidly units: average recovery rate in percentage per time<br>Simple and straightforward metrics, easy for comparisons |
| Bruneau et al. (2003)       | Loss of resilience R'<br>$R' = \int_{t_0}^{t_1} [100-Q(t)]dt$ | Q(t): the infrastructure quality, or performance of a system at a given time t.<br>t <sub>0</sub> : the time of incident or disturbance occurrence.<br>t <sub>1</sub> : time when restoration is completed (quality of infrastructure is 100%). | R' corresponds to the area above the resilience curve measured from t <sub>0</sub> to t <sub>1</sub>  |
| Bruneau and Reinhorn (2007) | Resilience R<br>$R = \int_{t_0}^{t_1} Q(t)dt$                 | See symbols in Figure 1   | R corresponds to the area below the resilience curve measured from t <sub>0</sub> to t <sub>1</sub>   |
| Attoh-Okine et al. (2007)   | $R = \frac{\int_{t_0}^{t_1} Q(t)dt}{100(t_1-t_0)}$            | Same as above   | Units: performance per unit time, where performance can be measured in percent (Figure 1).  |
| Cimellaro et al. (2009)     | $R = \frac{\int_{t_0}^{t_h} Q(t)dt}{(t_h-t_0)}$               | t <sub>h</sub> : time horizon (for a portfolio of bridges this can be the maximum recovery time).   | R is calculated for a larger period t <sub>h</sub> (or time horizon), so that a faster recovery results to higher values of R.                          |

Figure 1: Resilience model

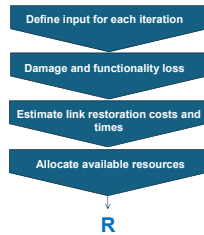
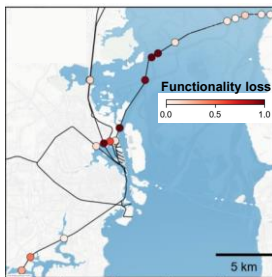


Source: Argyroudis, 2022

### Resilience-based decision making

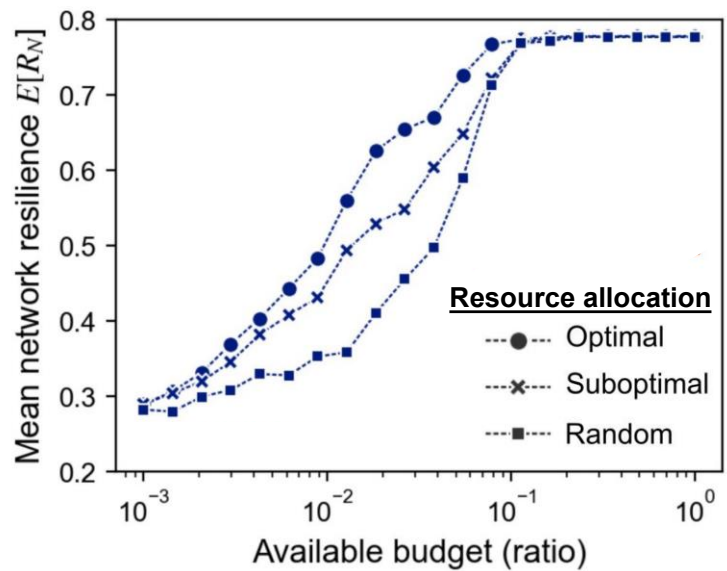


### Resilience-based decision making



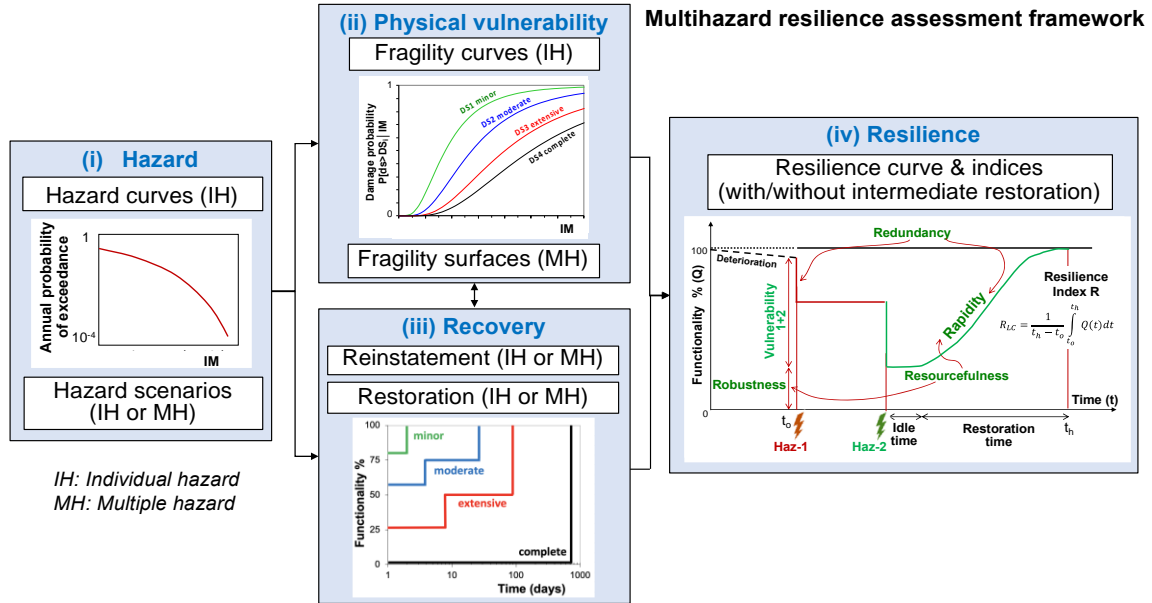
→ Allocating randomly results in significant lower R

→ Diminishing returns on R as the budget increases



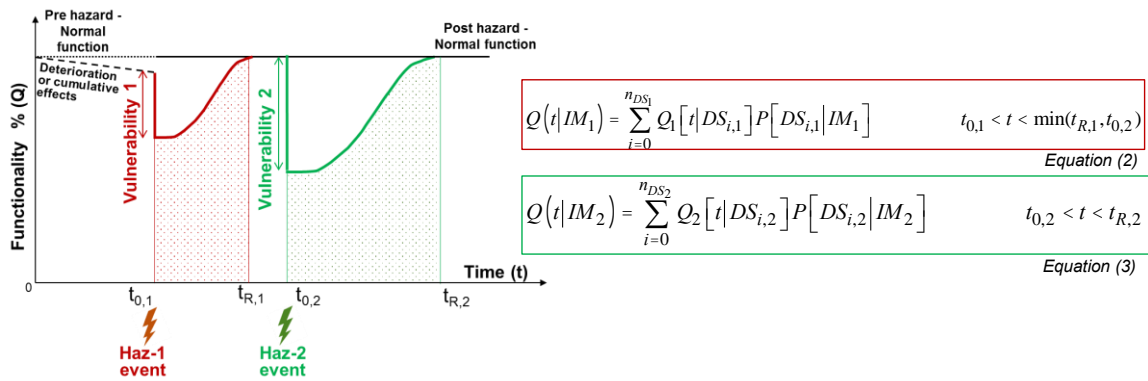
### Case studies

#### Multihazard resilience assessment framework



### Case studies

#### Resilience assessment for multiple hazards: restoration after Haz-1 and before Haz-2



**Vulnerability 1:** fragility functions for the initial or deteriorated asset

**Vulnerability 2:** fragility functions for the retrofitted asset

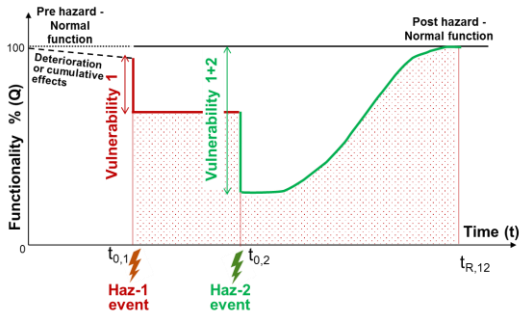
$$\left( \begin{matrix} < \\ \geq \\ | \\ = \\ > \end{matrix} \right) = \Phi \left( \frac{(-)}{(-)} \right) \quad \text{Equation (1)}$$

#### Resilience Index

$$R = \frac{1}{t_{R,2} - t_{0,1}} \int_{t_{0,1}}^{t_{R,2}} Q(t) dt$$

### Case studies

#### Resilience assessment for multiple hazards: without restoration after Haz-1 and before Haz-2 occurs



$$Q(t | IM_2) = \sum_{i=0}^{n_{DS1}} \sum_{j=0}^{n_{DS2}} Q_{12} [t | DS_{i,1}, DS_{j,2}] P [DS_{j,2} | DS_{i,1}, IM_2] \quad t_{0,2} < t < t_{R,12}$$

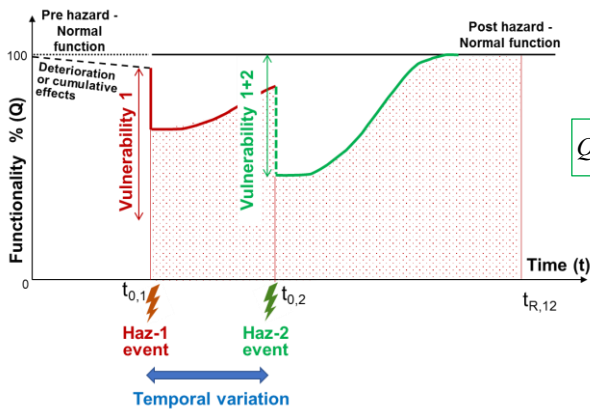
Equation (4)

**Vulnerability 1:** fragility functions for the **initial or deteriorated** asset

**Vulnerability 1+2:** fragility functions for the **damaged** asset (*state-dependent fragility functions are needed*)

### Case studies

#### Resilience assessment for multiple hazards: Haz-2 occurs before the restoration due to Haz-1 is completed



$$Q_{12} [t | DS_{i,1}, DS_{j,2}] = Q_1 (t | IM_1) - \left\{ 1 - Q_2 [t - t_{02} | DS_{i,1}, DS_{j,2}, t_{02}] \right\}$$

Equation (6)

$$\text{Resilience Index} = \frac{1}{.12 - .01} \int_{.01}^{.12} ( )$$

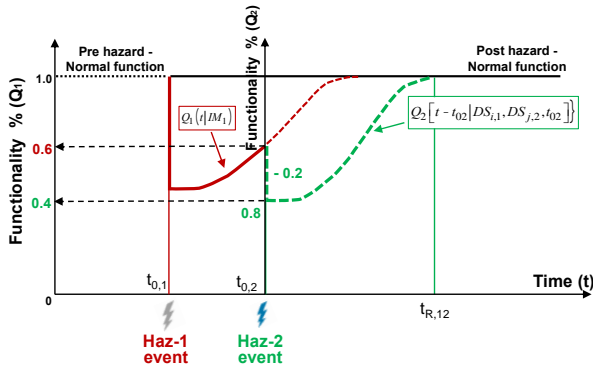
**Vulnerability 1:** fragility functions for the **initial or deteriorated** asset

**Vulnerability 1+2:** fragility functions for the **damaged/partially restored** asset

### Case studies

#### Resilience assessment for multiple hazards:

**Haz-2 occurs before the restoration due to Haz-1 is completed**



**Note:**

The loss of functionality  $Q_1$  (capacity) due to Haz-1 does not cause the same loss of functionality (capacity) for the effects of Haz-2,  $Q_2$  (due to different intensity and bridge condition)

$$Q_{12} [t | DS_{i,1}, DS_{j,2}] = Q_1 (t | IM_1) - \{ 1 - Q_2 [t - t_{02} | DS_{i,1}, DS_{j,2}, t_{02}] \}$$

$$= 0.6 - (1 - 0.8) = 0.4$$

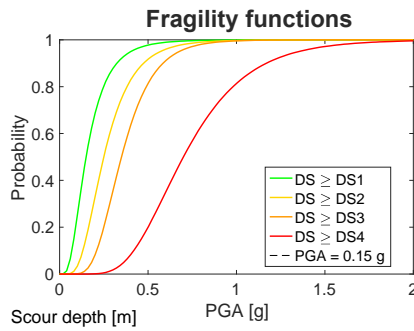
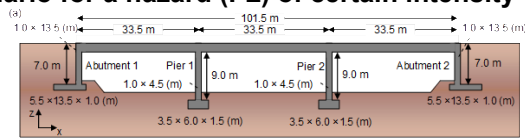


Argyroudis, Mitoulis et al. 2020

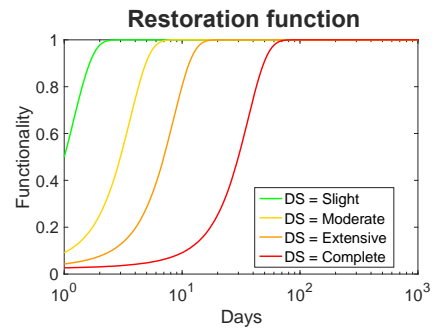
### Case studies

#### Example 1:

**Restoration of functionality after a scenario for a hazard (FL) of certain intensity**



| Fragility curves |            |       |
|------------------|------------|-------|
| Damage State     | Median (m) | Sigma |
| Slight           | 0.15       | 0.6   |
| Moderate         | 0.25       | 0.5   |
| Extensive        | 0.35       | 0.4   |
| Collapse         | 0.7        | 0.4   |



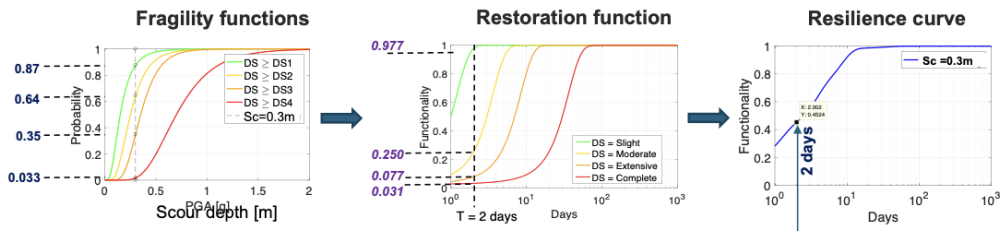
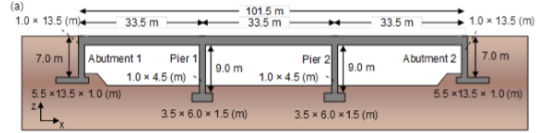
| Restoration curves |             |              |
|--------------------|-------------|--------------|
| Damage State       | Mean (days) | Sigma (days) |
| Slight             | 1           | 0.5          |
| Moderate           | 3           | 1.5          |
| Extensive          | 7           | 3.5          |
| Collapse           | 30          | 15           |



### Case studies

**Example 1:**  
**Restoration of functionality after a scenario for a hazard (FL) of certain intensity (Sc=0.3m)**

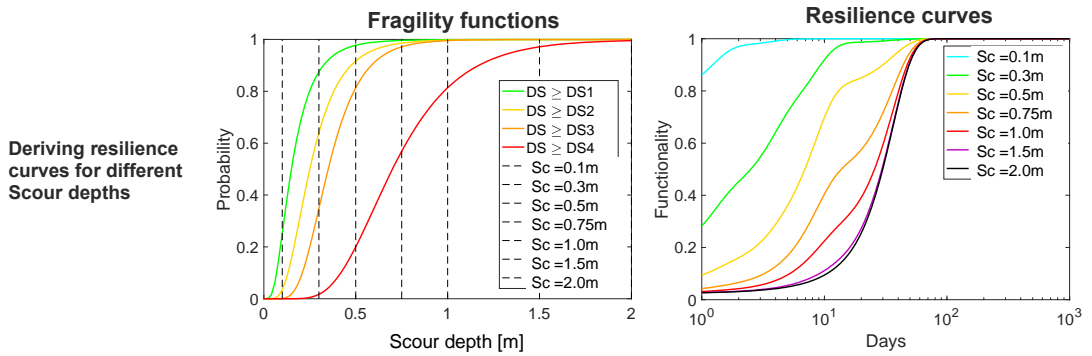
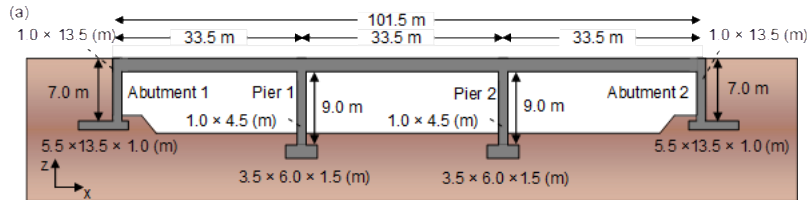
$$F[T = t] = \sum_{i=1}^{n_{DS}} F[DS_i, T = t] * P[DS_i]$$



$$F(t=2days) = 0.13 \times 1 + 0.23 \times 0.977 + 0.29 \times 0.250 + 0.317 \times 0.077 + 0.033 \times 0.031 = 0.452$$

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 1-0.87      0.87-0.64

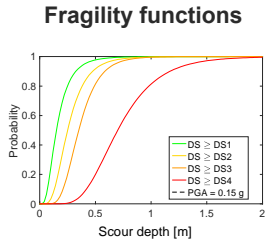
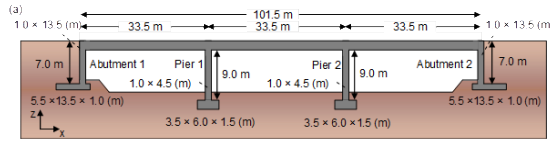
**Example 2:**  
**Restoration of functionality after 7 different scenarios (and hazard intensities)**



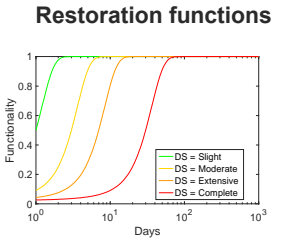
Deriving resilience curves for different Scour depths

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### Example 3: Improving resilience of a bridge with different restoration strategies

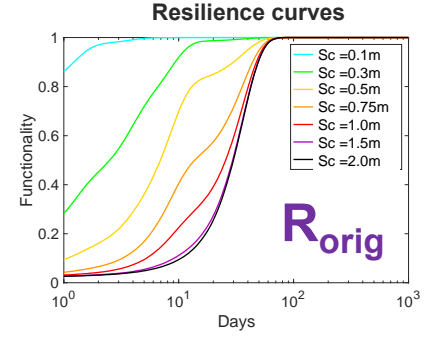


| Damage State | Median (m) | Sigma |
|--------------|------------|-------|
| Slight       | 0.15       | 0.6   |
| Moderate     | 0.25       | 0.5   |
| Extensive    | 0.35       | 0.4   |
| Collapse     | 0.7        | 0.4   |



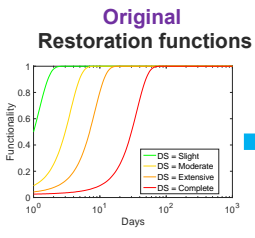
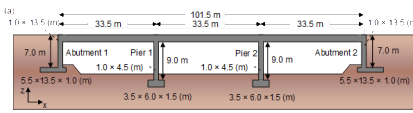
| Damage State | Mean (days) | Sigma (days) |
|--------------|-------------|--------------|
| Slight       | 1           | 0.5          |
| Moderate     | 3           | 1.5          |
| Extensive    | 7           | 3.5          |
| Collapse     | 30          | 15           |

#### Original restoration strategy

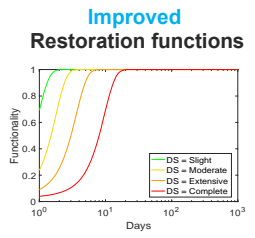


### Case studies

#### Example 3: Improving resilience of a bridge with different restoration strategies

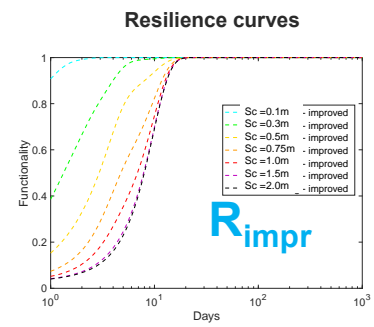


| Damage State | Mean (days) | Sigma (days) |
|--------------|-------------|--------------|
| Slight       | 1           | 0.5          |
| Moderate     | 3           | 1.5          |
| Extensive    | 7           | 3.5          |
| Collapse     | 30          | 15           |



| Damage State | Mean (days) | Sigma (days) |
|--------------|-------------|--------------|
| Slight       | 0.8         | 0.4          |
| Moderate     | 1.5         | 0.7          |
| Extensive    | 3           | 1.5          |
| Collapse     | 8           | 4            |

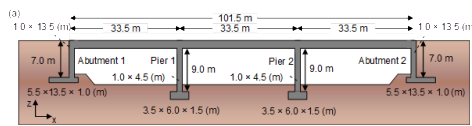
#### Improved restoration strategy



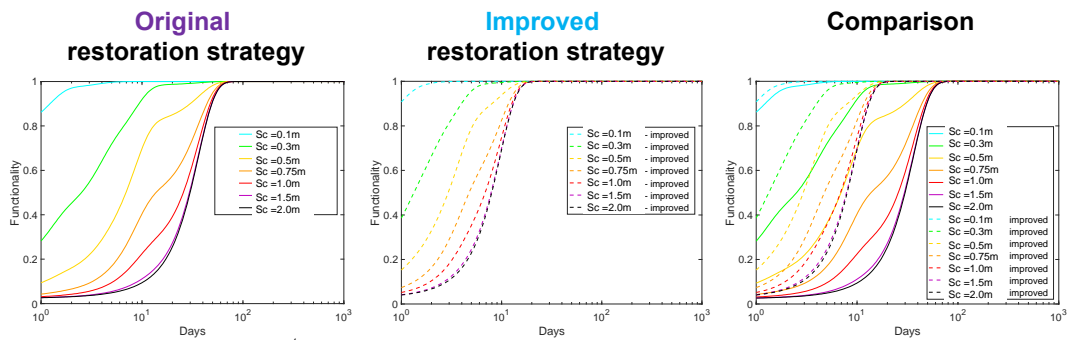


## Case studies

### Example 3: Improving resilience of a bridge with different restoration strategies



Resilience curves



$$R = \frac{1}{t_h - t_0} \int_{t_0}^{t_h} Q(t) dt$$

$$R_{orig} < R_{impr}$$



## Case study

### Resilience quantification:

- Step by step quantification of resilience for critical infrastructure considering different hazard and adaptation scenarios

